## Maximal Regularity for the Instationary Stokes System in an Aperture Domain

Andreas Fröhlich

Darmstadt University of Technology, Schlossgartenstr. 7, D-64289 Darmstadt, Germany, email: froehlich@mathematik.tu-darmstadt.de

## Abstract

We prove estimates in  $L^s(0,T; L^q_{\omega}(\Omega))$  for the solution of the instationary Stokes system in an aperture domain, where  $1 < s, q < \infty$  and the weight function  $\omega$  is in the Muckenhoupt class  $A_q$ .

The result is achieved by combining a characterisation of maximal regularity by  $\mathcal{R}$ -bounded operator families with the fact that  $\mathcal{R}$ -boundedness follows from weighted estimates for Muckenhoupt weights.

AMS classification: 35Q30, 35D05, 47D06

## 1 Introduction

Let  $d \ge 0$ ,  $n \ge 2$  and  $\mathbb{R}^n_{\pm} = \{x = (x_1, \ldots, x_n) \in \mathbb{R}^n : \pm x_n > d/2\}$ . Then an open connected set  $\Omega \subset \mathbb{R}^n$  is called an aperture domain if there is a ball  $B = B_R$  of radius R > 0 such that  $\Omega \cup B = \mathbb{R}^n_+ \cup \mathbb{R}^n_- \cup B$ .

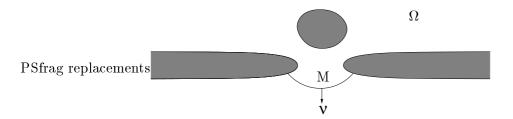


Figure 1: An aperture domain

In an aperture domain  $\Omega \subset \mathbb{R}^n$  we consider the instationary Stokes system

$$u_t - \Delta u + \nabla p = f \tag{1}$$

$$\operatorname{div} u = 0 \tag{2}$$

$$u\big|_{\partial\Omega} = 0 \tag{3}$$

$$u(0) = u_0. (4)$$

Heywood [16] pointed out that in order to single out a unique solution in the  $L^2$ -theory an additional auxiliary condition must be imposed. For example the flux  $\Phi(u) = \int_M u \cdot \nu \, d\sigma$  through aperture can be prescribed, where M is a smooth bounded (n-1)-dimensional